Let $\Sigma = \{0, 1\}$. Design a DFA for the following language.

$L = \{w \mid w \text{ does not contain the substring } 100110 \}$

You can present your design, just by depicting the state diagram clearly. No need to specify it formally. However, you must include a brief justification of the correctness of your design.